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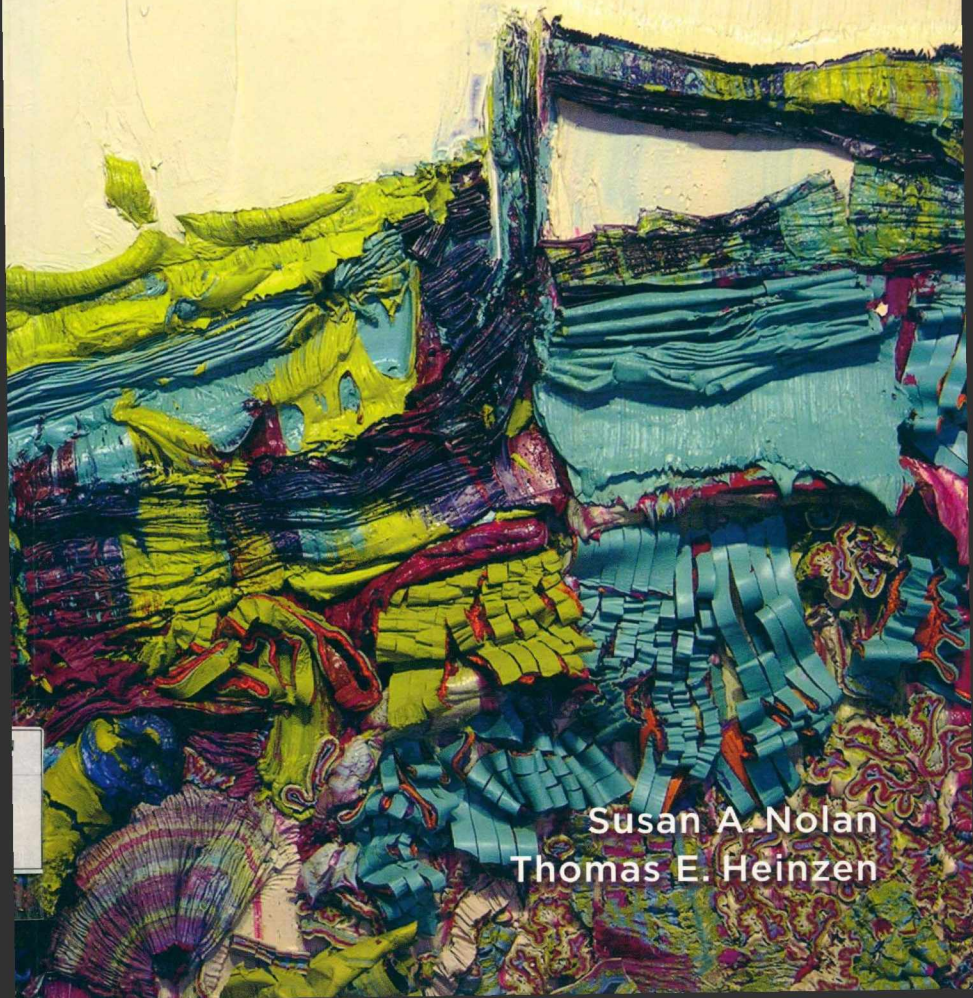
Statistics for the Behavioral Sciences



Susan A. Nolan
Thomas E. Heinzen

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Statistics for the Behavioral Sciences

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Leslie Wayne was born in Germany in 1953 and grew up in California. She received her BFA from Parsons School of Design in 1984. She is the recipient of a 2006 New York Foundation for the Arts Fellowship in Painting, and has received grants from the Pollock-Krasner Foundation, the New York State Council on the Arts, Adolph and Esther Gottlieb Foundation and the Buhl Founda-tion. Her work is in the public collections of The Foundation To-Life, Inc., the Birmingham Museum of Art, Colleczion Thyssen Bornemisza, the Corcoran Gallery of Art, La Coleccion Jumex in Mexico City, Harvard University, the Museum of Contemporary Art in Miami, The Neuberger Museum, and the University of Florida in Gainesville, among others. She exhibits regularly across the country and in Europe. She is represented by Jack Shainman Gallery in New York City.

For Ivan
—Susan

For Donna
—Tom

ABOUT THE AUTHORS

Susan Nolan turned to psychology after suffering a career-ending accident on her second workday as a bicycle messenger. A native of Boston, she graduated from The College of the Holy Cross and earned her PhD in clinical psychology from Northwestern University. Her research involves experimental investigations of the role of gender in the interpersonal consequences of depression and studies of gender and mentoring in science and technology, funded in part by the National Science Foundation. Susan is the Associate Dean of Graduate Studies for the College of Arts and Sciences, as well as an Associate Professor of Psychology, at Seton Hall University in New Jersey. She has served as a statistical consultant to researchers at several universities, medical schools, corporations, and non-governmental organizations. Recently, she advised Bosnian high school students conducting public opinion research.

Susan's academic schedule allows her to pursue one travel adventure per year, a tradition that she relishes. In recent years she rode her bicycle across the United States (despite her earlier crash), swapped apartments to live in Montreal, and explored the Adriatic coast in an intermittently roadworthy 1985 Volkswagon Scirocco. She wrote much of this book while spending a sabbatical year in rural Bosnia-Herzegovina, where her husband, Ivan Bojanic, worked as an advisor to regional governments. Susan and Ivan fell in love with Bosnia—a beautiful country—and bought a small house in the city of Banja Luka as a base for future adventures. They currently reside in New York City, where Susan roots feverishly, if quietly, for the Red Sox.

Tom Heinzen was a 29-year-old college freshman, began graduate school when his fourth daughter was one week old, and is still amazed that he and his wife, Donna, somehow managed to stay married. A magna cum laude graduate of Rockford College, he earned his PhD in social psychology at the State University of New York at Albany in just three years. He published his first book on frustration and creativity in government two years later, was a research associate in public policy until he was fired over the shape of a graph, consulted for the Johns Hopkins Center for Talented Youth, and then began a teaching career at William Paterson State University of New Jersey. He founded the psychology club, established an undergraduate research conference, and has been awarded various teaching honors while continuing to write journal articles, books, plays, and two novels that support the teaching of general psychology and statistics. He is also the editor of *Many Things to Tell You*, a volume of poetry by elderly writers.

His wife, Donna, is a physician assistant who has also volunteered her time in relief work following Hurricane Mitch and Hurricane Katrina. Their daughters are now scattered from Bangladesh to Mississippi to New Jersey and work in public health, teaching, and medicine. He is a mediocre French horn player, an enthusiastic but mediocre tennis player, and an ardent baseball fan (Go Cubs!).

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